

Polymath Software Report

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CACHE Trustee's Meeting
Notre Dame University
June 19, 2014

POLYMATH – Brief History

- **CACHE Site Licenses Started in 1990**
- **Polymath Software 2014**
Currently ~ 125+ paid CACHE site licenses plus ~ 40 institutions in developing countries, used with seven textbooks, personal educational and professional versions available via Internet sales
- **Himmelblau Award of CAST Division to authors 2010**

Current CACHE Site Licenses (now into 25th year)

Site licenses for POLYMATH software are available through the CACHE Corporation to academic departments (mostly CHEG) to some engineering colleges and schools. Computer labs, networks, faculty, and staff receive copies on an annual basis.

Current CACHE supporting departments pay \$175 for the first year and \$125 for each successive year thereafter. CACHE nonmember institution rates are an initial \$300 for the first year and a \$250 annual fee for subsequent years.

POLYMATH Individual Educational Licenses

- **Internet Sales Currently**
4-months \$20
12-months \$30
Unlimited use \$39
- **Special Sales with Textbooks Using Polymath at 50% of the Prices Given Above**
Thus a student with the latest Cutlip, Fogler, and Himmelblau books can get over a semester of unlimited use for ONLY \$10.

POLYMATH Individual Professional License

- **Unlimited use \$189**

POLYMATH Current Activities

- **POLYMATH 6.2 Educational Site License**
Version now included Limited DIPPR Database and User Interface at no cost.
- **DIPPR Add-On May be made Available**
 - Educational Site License Add-On \$700/YR
 - Single User Educational License Add-On \$100/YR
 - Single User Professional License Add-On \$300/YR
- **POLYMATH 7 under Development and Class Testing Underway – Completely .NET 4.0 code**

POLYMATH 7 Coming in 2014

- 1. Linear Programming – New Simplex Solver**
- 2. Nonlinear Equations – Automated Creation of complete MATLAB m-files**
- 3. Differential Equations – Output Options, Creation of MATLAB m-file, Tabular Outputs at Desired Intervals, Export to Excel with ODE Solver Add-In**
- 4. Simulation with Parameter Estimation in Dynamical Systems**
- 5. DIPPR Database Interface for Constant and Variable Properties with output to Polymath, MATLAB and Excel**

PolyMathLite is Coming to Android is here!!!!

www.polymathlite.com



Polymath Light

✓ Check Examples ▾ Settings

Solve 2 nonlinear equations:
$2*x+x*y-y^2 = -290$
$x*\log(y/2)+x*y = 105$
Using the initial guess: $x(0)=2, y(0)=10$
The solution should be: $x=5, y=20$

$f(x) = 2*x+x*y-y^2 + 290$
 $f(y) = x*\log(y/2)+x*y - 105$
 $x(0)=2$
 $y(0) = 10$

Ln: 1 Col: 1

POLYMATL Report NLE
Nonlinear Equations 2013-Apr-19

Calculated values of NLE variables

	Variable	Value	f(x)	Initial Guess	Initial f(x)
1	x	5	-2.7E-12	2	2.1E02
2	y	20	1.3E-12	10	-8.4E01

Nonlinear equations

- $f(x) = 2*x+x*y-y^2 + 290 = 0$
- $f(y) = x*\log(y/2)+x*y - 105 = 0$



Polymath Report

POLYMATL Report NLE
Nonlinear Equation 2013-Apr-19

Calculated values of NLE variables

	Variable	Value	f(x)	Initial Guess	Initial f(x)
		0.015782	1.7E-11	0.02505	4.9E00

	Variable	Value	Initial Value
1	CD	8.84266	6.11879
2	Dp	0.000208	0.000208
3	g	9.80665	9.80665
4	Re	3.65564	5.80256
5	rho	994.6	994.6
6	rhop	1800	1800
7	vis	0.000893	0.000893

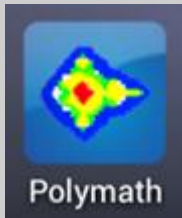
Nonlinear equations

- $f(vt) = vt^2*(3*CD*rho)-4*g*(rhop-rho)*Dp = 0$

Explicit equations

- $rho = 994.6$
- $g = 9.80665$

Android Based PolyMathLite

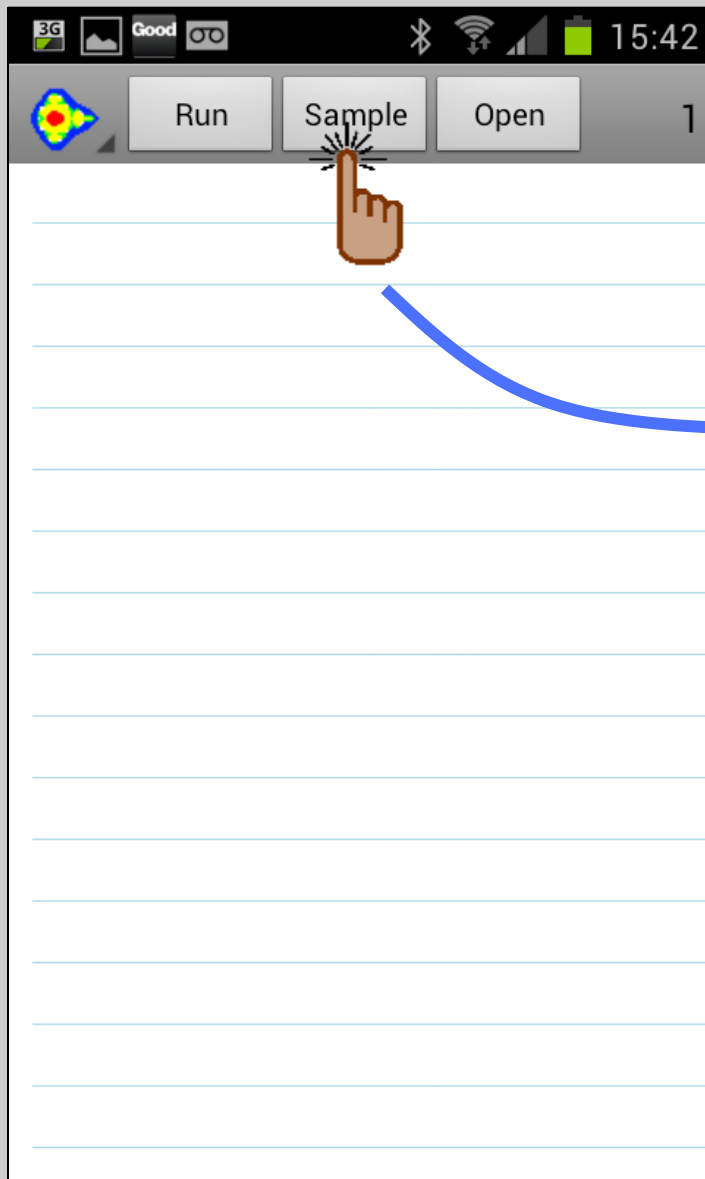


Polymath Lite

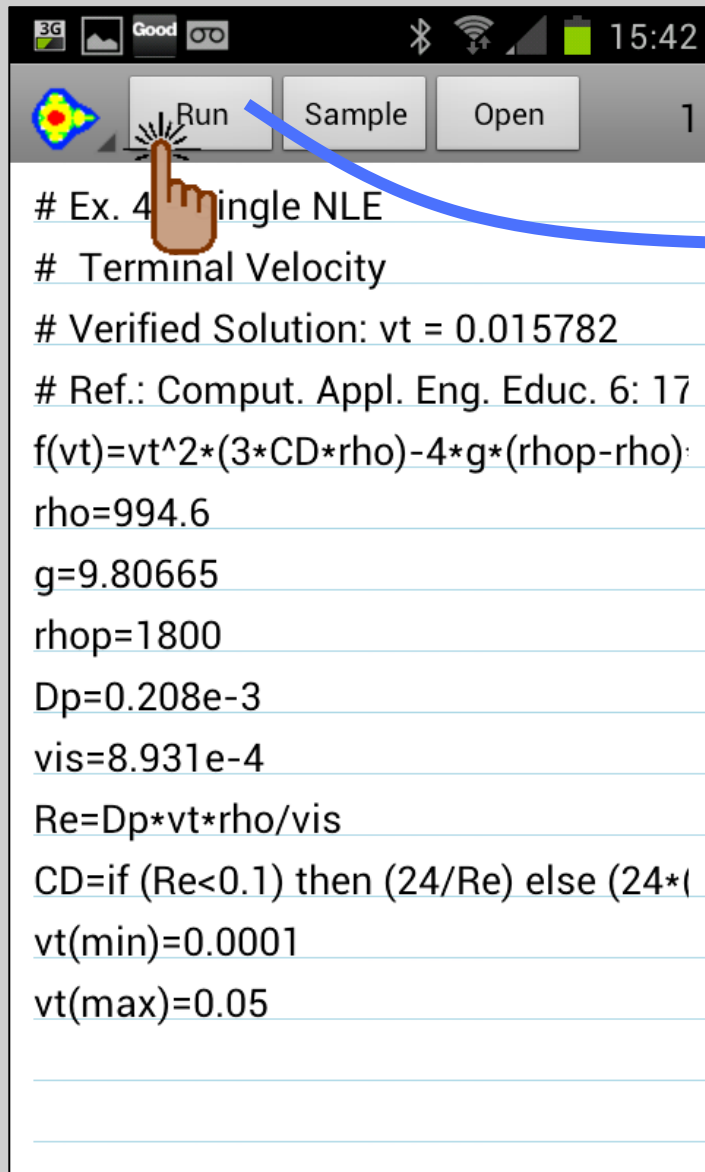
Same program syntax for NLE, DEQ
Simplified Syntax for LEQ
Simplified Syntax for REG
Access to Chart Software
Direct Conversion to Matlab
Sharing Options via E-mail
and Bluetooth



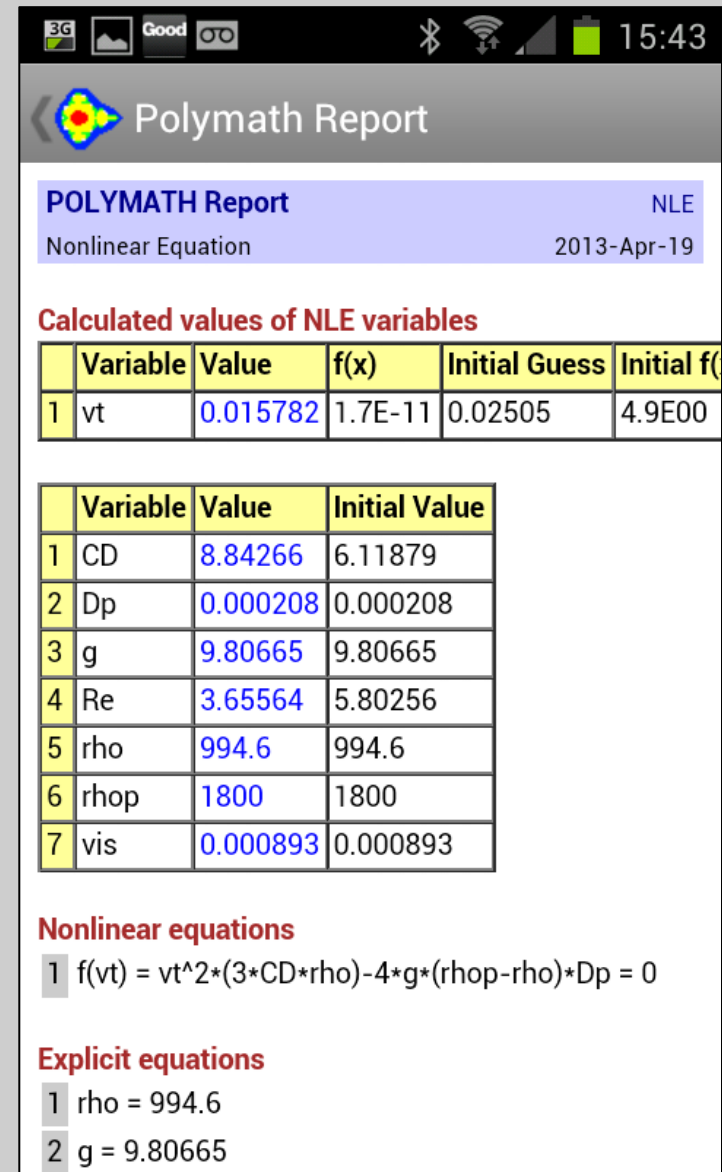
Home Screen, Open Sample



Edit Program, Run Program, Get Solution Report



```
# Ex. 4 Single NLE
# Terminal Velocity
# Verified Solution: vt = 0.015782
# Ref.: Comput. Appl. Eng. Educ. 6: 17
f(vt)=vt^2*(3*CD*rho)-4*g*(rhop-rho)
rho=994.6
g=9.80665
rhop=1800
Dp=0.208e-3
vis=8.931e-4
Re=Dp*vt*rho/vis
CD=if (Re<0.1) then (24/Re) else (24*(
vt(min)=0.0001
vt(max)=0.05
```



POLYMATH Report NLE
Nonlinear Equation 2013-Apr-19

Calculated values of NLE variables

	Variable	Value	f(x)	Initial Guess	Initial f(x)
1	vt	0.015782	1.7E-11	0.02505	4.9E00

	Variable	Value	Initial Value
1	CD	8.84266	6.11879
2	Dp	0.000208	0.000208
3	g	9.80665	9.80665
4	Re	3.65564	5.80256
5	rho	994.6	994.6
6	rhop	1800	1800
7	vis	0.000893	0.000893

Nonlinear equations

1 $f(vt) = vt^2 \cdot (3 \cdot CD \cdot \rho) - 4 \cdot g \cdot (\rho_{hop} - \rho) \cdot D_p = 0$

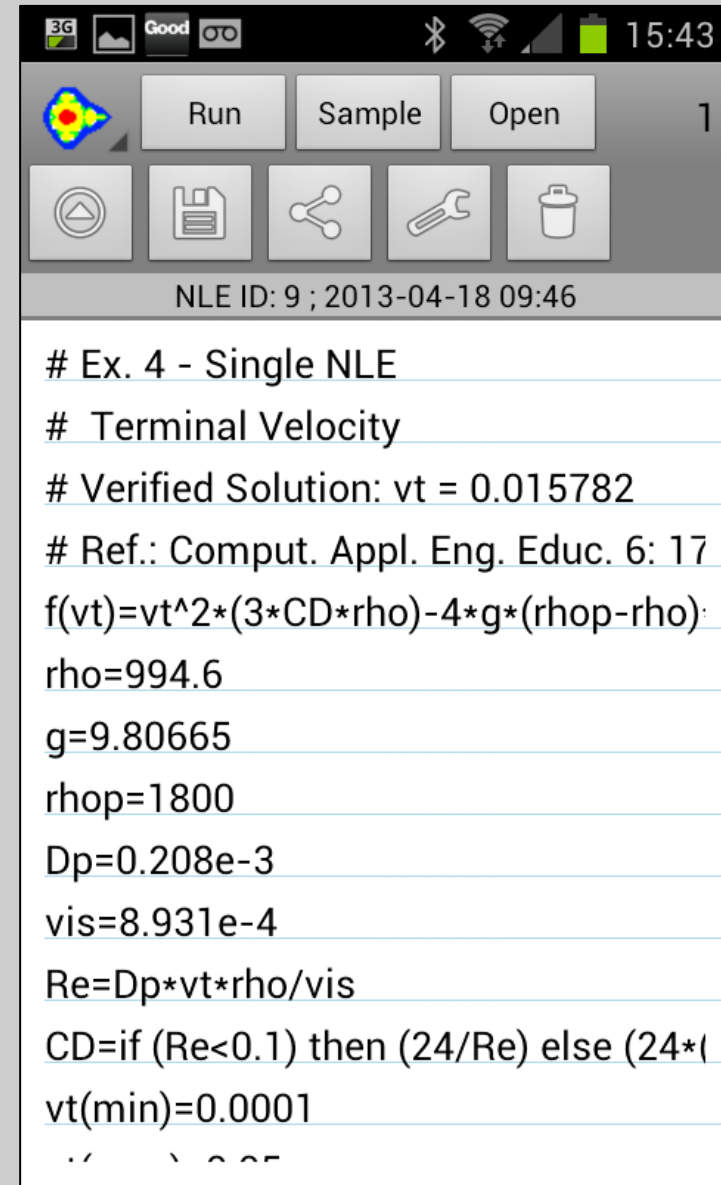
Explicit equations

1 $\rho = 994.6$
2 $g = 9.80665$

Open Saved File, Save/Share/Settings Buttons



Open Polymath File		
Ex. 1 - Linear Eqs.		
LEQ	2	2013-04-18 00:38
Ex. 2 - Single NLE		
NLE	6	2013-04-18 09:46
Ex. 2 - Single NLE		
NLE	7	2013-04-18 09:46
Ex. 3 - Simultaneous NLEs		
NLE	1	2013-04-18 00:38
Ex. 3 - Simultaneous NLEs		
NLE	8	2013-04-18 09:46
Ex. 4 - Single NLE		
NLE	9	2013-04-18 09:46
Ex. 4 - Single NLE		
NLE	10	2013-04-18 09:46
Ex. 5 - NLE System		
NLE	3	2013-04-18 00:38
Ex. 5 - NLE System		
NLE	5	2013-04-18 01:12



Run Sample Open 1

NLE ID: 9 ; 2013-04-18 09:46

```
# Ex. 4 - Single NLE
# Terminal Velocity
# Verified Solution: vt = 0.015782
# Ref.: Comput. Appl. Eng. Educ. 6: 17
f(vt)=vt^2*(3*CD*rho)-4*g*(rhop-rho):
rho=994.6
g=9.80665
rhop=1800
Dp=0.208e-3
vis=8.931e-4
Re=Dp*vt*rho/vis
CD=if (Re<0.1) then (24/Re) else (24*(
vt(min)=0.0001
```

Settings Screen





Polymath Light for Android

Polymath is a proven computational system, which has been specifically created for educational or professional use. It allows the user to apply effective numerical analysis techniques during interactive problem solving on Android OS smart phones and Tablets.

Results are presented with a standard html based report for easy understanding and can be shared across for incorporation into mail messages, papers, and reports. Students, engineers, mathematicians, scientists, or anyone with a need to problems will appreciate the efficiency and speed of problem solution.

This Help will enable you to start using Polymath for engineering problem solving. For advanced applications please refer also to PolyMathLite User's Manual which is available at the website: www.polymathlite.com

Content:



Polymath Help

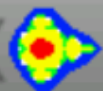
applications please refer also to PolymathLite User's Manual which is available at the website: www.polymathlite.com

Content:



- [Main Problem Entry Screen](#)
- [Linear Equations](#)
- [Nonlinear Equations](#)
- [Ordinary Differential Equations](#)
- [Polynomial Regression](#)
- [Multiple linear Regression](#)
- [Nonlinear Regression](#)
- [Polymath Control Buttons](#)
- [Built in Samples Screen](#)
- [Variables and Expressions](#)

Main Problem Entry Screen



Polymath Help

$\exp(3 \cdot 5 \cdot \log(6))$

Condition Operator

These operators return "1" if the condition met, and "0" if the condition does not meet.
Examples: The expression '3>6' returns 0. The expression '4>=4' returns 1.

Valid conditional operators:

>, <, >=, <=, ==

Boolean Operator

The Boolean operators return "1" if the condition is met, and "0" if the condition is not met.
Example: The expression '(2>3) or (1>0)' returns 1. The expression '1 and 0' returns 0.

Valid Boolean operators:

And, Or

If-Then-Else

There are three case-insensitive keywords which compose the if-then-else expression structure.

The three keywords are: If, Then, Else.

Samples:

If (2>5) Then (sin(12)+4) Else (sin(12)+8)

if(2>5)then(sin(12)+4)else(sin(12)+8)

Open Parenthesis: (

Close Parenthesis:)



Polymath Help

A special 'if' statement is available, with the following syntax:

```
if (condition) then (expression1) else (expression2)
```

The parentheses are optional.

The condition may include the following operators: and, or (Boolean operators), > (greater than), < (less than), >= (greater than or equal), <= (less than or equal), == (equals).

The expressions may be any formula, including another 'if' statement.

For example:

```
A = if (x>0) then (log(x)) else(0)
b = if (T<minT) then (minT) else (if (T>maxT) then (maxT) else
(T))
Vol_h1 = if (a>5 and c<2) then 1.12 else 7.89
```

Available Functions

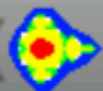


Polymath Help

Available Functions

A number of standard functions are available for use in the various programs. The arguments of the functions must be enclosed in parentheses. The arguments may be themselves expressions or other functions. The nesting of functions is allowed.

Function Name	Description
abs ()	absolute value
arccos ()	trigonometric inverse cosine with result in radians
arccosec ()	trigonometric inverse cosecant with result in radians
arccosech ()	inverse hyperbolic cosecant
arcsech ()	inverse hyperbolic secant
arccosh ()	inverse hyperbolic cosine
arccotan ()	trigonometric inverse cotangent with result in radians
arccotanh ()	inverse hyperbolic cotangent
arcsin ()	trigonometric inverse sine with result in radians



Polymath Help

cosec ()	trigonometric cosecant with argument in radians
cosech ()	hyperbolic cosecant
cosh ()	hyperbolic cosine
cotan ()	trigonometric cotangent with argument in radians
coth ()	hyperbolic cotangent
exp ()	exponential (e^x)
erf ()	error function
exp10 ()	exponential of 10 (10^x)
exp2 ()	exponential of 2 (2^x)
fact (N)	factorial of integer part of number N (this only operates on a number)
frac ()	fractional part
int ()	integer part
ln ()	natural logarithm to the base e
log ()	logarithm to the base 10
psi ()	psi function



Polymath Sample Programs



Ex. 1 - Linear Eqs.

Steady State Material Balances



Ex. 2 - Single NLE

Molar Volume and Compress... Van Der Waals



Ex. 3 - NLE System

Three Phase Equilib.



Ex. 4 - Single NLE

Terminal Velocity



Ex. 5 - NLE System

Reaction Equilibrium



Ex. 6 (a) - Fitting Polynomials

Pressure Data



Ex. 6 (b) - Linear Regression

Pressure Data



Ex. 6 (c) - Nonlinear Regression

Pressure Data



Ex. 7 - ODE System

Heat Exchange



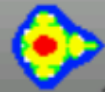
Ex. 8- Boundary Value ODE System

Diffusion with Reaction



Ex. 9 - ODE System

Reversible Reaction in a PBR



Run

Sample

Open

1



Ex. 2 - Single NLE

Molar Volume and Compress... Van Der Waals

Verified Solution: $V=0.574892$, $Z=0.871827$

Ref.: Comput. Appl. Eng. Educ. 6: 171-172, 1998

$f(V)=(P+a/(V^2))*(V-b)-R*T$

$P=56$

$R=0.08206$

$T=450$

$T_c=405.5$



Polymath Report

POLYMATH Report

Nonlinear Equation

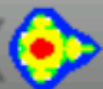
NLE

2013-Jun-14

Calculated values of NLE variables

	Variable	Value	f(x)	Initial Guess	Initial f(x)
1	V	0.574892	9.5E-11	0.7	5.9E00

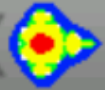
	Variable	Value	Initial Value
1	a	4.19695	4.19695
2	b	0.037371	0.037371
3	P	56	56
4	Pc	111.3	111.3
5	Pr	0.503145	0.503145
6	P	0.08206	0.08206



Polymath Report

	Variable	Value	f(x)	Initial Guess	Initial f(x)
1	V	0.574892	9.5E-11	0.7	5.9E00

	Variable	Value	Initial Value
1	a	4.19695	4.19695
2	b	0.037371	0.037371
3	P	56	56
4	Pc	111.3	111.3
5	Pr	0.503145	0.503145
6	R	0.08206	0.08206
7	T	450	450
8	Tc	405.5	405.5
9	Z	0.871827	1.06155



Polymath Report

Nonlinear equations

1 $f(V) = (P + a/(V^2)) * (V - b) - R * T = 0$

Explicit equations

1 $P = 56$

2 $R = 0.08206$

3 $T = 450$

4 $T_c = 405.5$

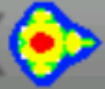
5 $P_c = 111.3$

6 $Pr = P/P_c$

7 $a = 27 * (R^2 * T_c^2 / P_c) / 64$

8 $b = R * T_c / (8 * P_c)$

9 $Z = P * V / (R * T)$



Polymath Report

Problem source text

```
# Ex. 2 - Single NLE
# Molar Volume and Compress... Van Der Waals
# Verified Solution: V=0.574892, Z =0.871827
# Ref.: Comput. Appl. Eng. Educ. 6: 171-172, 1998
f(V)=(P+a/(V^2))*(V-b)-R*T
P=56
R=0.08206
T=450
Tc=405.5
Pc=111.3
Pr=P/Pc
a=27*(R^2*Tc^2/Pc)/64
b=R*Tc/(8*Pc)
Z=P*V/(R*T)
```



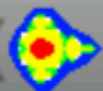

Polymath Report

Matlab formatted problem

Create m file called PolyNle.m and paste the following text into it.

```
% Polymath NLE problem conversion to Matlab
% NLE
function PolyNle
    xguess = 0.7 ;
    x = fzero(@NLEfun,xguess);
    fprintf('The NLE solution is %g\n', x);
end

function fV = NLEfun(V)
    P = 56;
    R = 0.08206;
    T = 450;
    Tc = 405.5;
    Pc = 111.3;
    Pr = P / Pc;
    a = 27 * R ^ 2 * Tc ^ 2 / Pc / 64;
    b = R * Tc / (8 * Pc);
    Z = P * V / (R * T);
    fV = (P + a / (V ^ 2)) * (V - b) - (R * T);
end
```



Polymath Report

```
Pr = P / Pc;  
a = 27 * R ^ 2 * Tc ^ 2 / Pc / 64;  
b = R * Tc / (8 * Pc);  
Z = P * V / (R * T);  
fV = (P + a / (V ^ 2)) * (V - b) - (R * T);  
end
```

General Settings

Total number of equations	10
Number of implicit equations	1
Number of explicit equations	9
Elapsed time	0.07 sec
Reporting digits	8
Solution method	safenewt
Max iterations	150
Tolerance F	1E-07
Tolerance X	1E-07
Tolerance min	1E-07

Data file: no file



Ex. 2 - Single NLE

Molar Volume and Compress... Van Der
Waals

Verified Solution: $V=0.574892$, $Z=0.871827$

Ref.: Comput. Appl. Eng. Educ. 6: 171-172,
1998

$$f(V) = (P + a/(V^2)) * (V - b) - R * T$$

$$P = 56$$

$$R = 0.08206$$

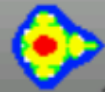
$$T = 450$$

$$T_c = 405.5$$

$$P_c = 111.2$$

Done





Run

Sample

Open

5



Ex. 2 - Single NLE

Molar Volume and Compress... Van Der Waals

Verified Solution: $V=0.574892$, $Z=0.871827$

Ref.: Comput. Appl. Eng. Educ. 6: 171-172, 1998

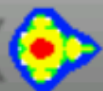
$f(V)=(P+a/(V^2))*(V-b))-R*T$

$P=56$

$R=0.08206$

$T=450$

$T_c=405.5$



Polymath Report

Errors in NLE

	Message
1	Error in Line #5, unequal number of parantheses. Too many ')'
2	Implicit variables (1) V
3	Explicit variables (9) P, R, T, Tc, Pc, Pr, a, b, Z
4	All variables (10) P, a, V, b, R, T, Tc, Pc, Pr, Z



Ex. 2 - Single NLE

Molar Volume and Compress... Van Der
Waals

Verified Solution: $V=0.574892$, $Z=0.871827$

Ref.: Comput. Appl. Eng. Educ. 6: 171-172,
1998

$$f(V) = (P + a/(V^2)) * (V - b) - R * T$$

$$P = 56$$

$$R = 0.08206$$

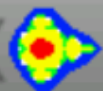
$$T = 450$$

$$T_c = 405.5$$

$$P_c = 111.3$$

Done

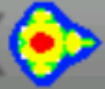




Polymath Report

Errors in NLE

	Message
1	1 Undefined variable exists; v
2	Implicit variables (1) V
3	Explicit variables (9) P, R, T, Tc, Pc, Pr, a, b, Z
4	All variables (11) P, a, V, v, b, R, T, Tc, Pc, Pr, Z



Polymath Sample Programs



Ex. 12 - Single Partial Diff. Eq.

Unsteady State Heat Conduction.



Ex. 13 - Nonlinear Regression

Catalytic Reforming Reac.



Ex. 14(a) - Multi-Linear Regression

Heat of Hardening



Ex. 14(b) - Multi-Linear Regression via origin

Heat of Hardening



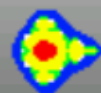
Ex. 15 - Linear Eqs.

Biological Reactors



Ex. 16 - Stiff ODE System

Biological Reactors



Run

Sample

Open

7

Ex. 12 - Single Partial Diff. Eq.

Unsteady State Heat Conduction.

Verified final values: $T_2 = 48.6618$, $T_4 = 52.644$

$T_6 = 50.7581$, $T_8 = 50.701$, $T_{10} = 50.9248$

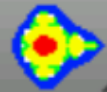
Ref.: Prob. 9.12 in Problem Solving in Chemical...

$$d(T_4)/dt = \alpha/\Delta x^2 * (T_5 - 2*T_4 + T_3)$$

$$d(T_5)/dt = \alpha/\Delta x^2 * (T_6 - 2*T_5 + T_4)$$

$$d(T_3)/dt = \alpha/\Delta x^2 * (T_4 - 2*T_3 + T_2)$$

$$d(T_6)/dt = \alpha/\Delta x^2 * (T_7 - 2*T_6 + T_5)$$



Run

Sample

Open

19

deltaTs=20

$\tau=365$

$t_0=37$

$T_{11}=T_m$

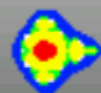
$T_s = T_m - \Delta T_s \cdot \cos\left(\left(2 \cdot 3.1416 / \tau\right) \cdot (t - t_0)\right)$

$T_1 = T_s$

$t(0)=0$

$T_4(0)=51$

$T_5(0)=51$



Run

Sample

Open

7

Ex. 12 - Single Partial Diff. Eq.

Unsteady State Heat Conduction.

Verified final values: $T_2 = 48.6618$, $T_4 = 52.644$

$T_6 = 50.7581$, $T_8 = 50.701$, $T_{10} = 50.9248$

Ref.: Prob. 9.12 in Problem Solving in Chemical...

$$d(T_4)/dt = \alpha/\Delta x^2 * (T_5 - 2*T_4 + T_3)$$

$$d(T_5)/dt = \alpha/\Delta x^2 * (T_6 - 2*T_5 + T_4)$$

$$d(T_3)/dt = \alpha/\Delta x^2 * (T_4 - 2*T_3 + T_2)$$

$$d(T_6)/dt = \alpha/\Delta x^2 * (T_7 - 2*T_6 + T_5)$$



Polymath Report

POLYMATH Report

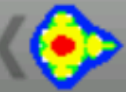
DEQ

Ordinary Differential Equations

2013-Jun-14

Calculated values of DEQ variables

	Variable	Initial value	Final value	Minimal value	Maximal value
1	alpha	0.9	0.9	0.9	0.9
2	deltaTs	25	25	25	25
3	deltax	8	8	8	8
4	t	0	365	0	365
5	t0	37	37	37	37
6	T1	30.9018	30.9016	26.0001	75.9937
7	T10	51	50.9248	50.9248	51
8	T11	51	51	51	51
9	T2	51	48.6618	39.6826	61.7579



Polymath Report

Differential equations

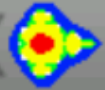
- 1 $d(T4)/d(t) = \alpha/\text{deltax}^2 \cdot (T5 - 2 \cdot T4 + T3)$
- 2 $d(T5)/d(t) = \alpha/\text{deltax}^2 \cdot (T6 - 2 \cdot T5 + T4)$
- 3 $d(T3)/d(t) = \alpha/\text{deltax}^2 \cdot (T4 - 2 \cdot T3 + T2)$
- 4 $d(T6)/d(t) = \alpha/\text{deltax}^2 \cdot (T7 - 2 \cdot T6 + T5)$
- 5 $d(T2)/d(t) = \alpha/\text{deltax}^2 \cdot (T3 - 2 \cdot T2 + T1)$
- 6 $d(T7)/d(t) = \alpha/\text{deltax}^2 \cdot (T8 - 2 \cdot T7 + T6)$
- 7 $d(T8)/d(t) = \alpha/\text{deltax}^2 \cdot (T9 - 2 \cdot T8 + T7)$
- 8 $d(T9)/d(t) = \alpha/\text{deltax}^2 \cdot (T10 - 2 \cdot T9 + T8)$
- 9 $d(T10)/d(t) = \alpha/\text{deltax}^2 \cdot (T11 - 2 \cdot T10 + T9)$

Explicit equations

- 1 $\alpha = 0.9$



1:22 AM



Polymath Report

Problem source text

```
# Ex. 12 - Single Partial Diff. Eq.  
# Unsteady State Heat Conduction.  
# Verified final values: T2= 48.6618, T4= 52.644  
# T6= 50.7581, T8= 50.701, T10= 50.9248  
# Ref.:Prob. 9.12 in Problem Solving in Chemical...  
d(T4)/d(t)=alpha/deltax^2*(T5-2*T4+T3)  
d(T5)/d(t)=alpha/deltax^2*(T6-2*T5+T4)  
d(T3)/d(t)=alpha/deltax^2*(T4-2*T3+T2)  
d(T6)/d(t)=alpha/deltax^2*(T7-2*T6+T5)  
d(T2)/d(t)=alpha/deltax^2*(T3-2*T2+T1)  
d(T7)/d(t)=alpha/deltax^2*(T8-2*T7+T6)  
d(T8)/d(t)=alpha/deltax^2*(T9-2*T8+T7)  
d(T9)/d(t)=alpha/deltax^2*(T10-2*T9+T8)  
d(T10)/d(t)=alpha/deltax^2*(T11-2*T10+T9)  
alpha=0.9  
deltax=8  
Tm=51
```



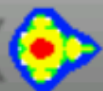
Polymath Report

Matlab formatted problem

Create m file called PolyOde.m and paste the following text into it.

```
% Polymath ODE problem conversion to Matlab
% DEQ
function PolyOde
    tspan = [0 365]; % Range for the independent variable
    y0 = [51; 51; 51; 51; 51; 51; 51; 51; 51]; % Initial values for the dependent variables
    [t,y]=ode45(@ODEfun,tspan, y0);
    plot (t,y);
    xlabel('t');
    legend('T4','T5','T3','T6','T2','T7','T8','T9','T10');
    fprintf('T4 = %16.6f \n',y(length(y),1));
    fprintf('T5 = %16.6f \n',y(length(y),2));
    fprintf('T3 = %16.6f \n',y(length(y),3));
    fprintf('T6 = %16.6f \n',y(length(y),4));
    fprintf('T2 = %16.6f \n',y(length(y),5));
    fprintf('T7 = %16.6f \n',y(length(y),6));
    fprintf('T8 = %16.6f \n',y(length(y),7));
    fprintf('T9 = %16.6f \n',y(length(y),8));
    fprintf('T10 = %16.6f \n',y(length(y),9));
end

function dYfuncvecdt = ODEfun(t,Yfuncvec)
```



Polymath Report

```
T7 = Yfuncvec(6);
T8 = Yfuncvec(7);
T9 = Yfuncvec(8);
T10 = Yfuncvec(9);
alpha = 0.9;
deltax = 8;
Tm = 51;
deltaTs = 25;
tau = 365;
t0 = 37;
T11 = Tm;
Ts = Tm - (deltaTs * cos(2 * 3.1416 / tau * (t - t0)));
T1 = Ts;
dT4dt = alpha / (deltax ^ 2) * (T5 - (2 * T4) + T3);
dT5dt = alpha / (deltax ^ 2) * (T6 - (2 * T5) + T4);
dT3dt = alpha / (deltax ^ 2) * (T4 - (2 * T3) + T2);
dT6dt = alpha / (deltax ^ 2) * (T7 - (2 * T6) + T5);
dT2dt = alpha / (deltax ^ 2) * (T3 - (2 * T2) + T1);
dT7dt = alpha / (deltax ^ 2) * (T8 - (2 * T7) + T6);
dT8dt = alpha / (deltax ^ 2) * (T9 - (2 * T8) + T7);
dT9dt = alpha / (deltax ^ 2) * (T10 - (2 * T9) + T8);
dT10dt = alpha / (deltax ^ 2) * (T11 - (2 * T10) + T9);
dYfuncvecdt = [dT4dt; dT5dt; dT3dt; dT6dt; dT2dt; dT7dt; dT8dt; dT9dt; dT10dt];
```

end



Polymath Report

General

Total number of equations 18
Number of differential equations 9
Number of explicit equations 9
Reporting digits 8
Elapsed time 0.30 sec
Solution method RKF_45
Step size guess. h 1E-06
Truncation error tolerance. eps 1E-06
Calculated Intermediate data points 50

Data file: no file

Calculated data points

	t	T4	T5	T3	T6	T2	T7	T8	T9	T10	T11	Ts	T1
1	0	51	51	51	51	51	51	51	51	51	51	30.9018	30.9018
2	16.7188	50.9674	50.9982	50.5598	50.9999	46.8263	51	51	51	51	51	27.9524	27.9524
3	22.5588	50.9273	50.9945	50.2582	50.9997	45.6043	51	51	51	51	51	27.1082	27.1082
4	34.2388	50.7897	50.9765	49.5305	50.9978	43.5003	50.9998	51	51	51	51	26.1195	26.1195



Polymath Report

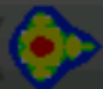
33	244.479	49.9593	49.6506	52.9726	50.1131	61.2682	50.5534	50.8104	50.9297	50.9783	51	74.2191	74.2191
34	250.319	50.1832	49.7177	53.3932	50.1134	61.5561	50.5391	50.7992	50.9238	50.976	51	73.1718	73.1718
35	256.159	50.4093	49.7918	53.7848	50.118	61.7347	50.5262	50.7882	50.9178	50.9737	51	71.9007	71.9007
36	267.839	50.8595	49.9587	54.4654	50.14	61.7579	50.5056	50.7671	50.9056	50.9686	51	68.7402	68.7402
37	273.679	51.0791	50.0499	54.7479	50.1571	61.6025	50.498	50.7573	50.8994	50.966	51	66.8827	66.8827
38	279.519	51.2923	50.1451	54.9879	50.1783	61.3374	50.4922	50.7479	50.8932	50.9633	51	64.8649	64.8649
39	285.359	51.497	50.2435	55.1831	50.2032	60.9655	50.4884	50.7392	50.887	50.9605	51	62.7071	62.7071
40	297.039	51.8731	50.4459	55.4321	50.2634	59.9171	50.4867	50.7236	50.875	50.9549	51	58.0597	58.0597
41	302.879	52.0408	50.5482	55.4835	50.2982	59.2514	50.4888	50.717	50.8692	50.952	51	55.6171	55.6171
42	308.719	52.1928	50.6497	55.4854	50.3357	58.5	50.4929	50.7112	50.8636	50.9492	51	53.1279	53.1279
43	314.559	52.3277	50.7497	55.4379	50.3755	57.6706	50.4988	50.7062	50.8582	50.9463	51	50.6173	50.6173
44	326.239	52.541	50.9411	55.1973	50.4606	55.8119	50.5162	50.6989	50.8483	50.9408	51	45.6328	45.6328
45	332.079	52.6174	51.0307	55.0068	50.5052	54.8016	50.5275	50.6966	50.8438	50.9381	51	43.2093	43.2093
46	337.919	52.6726	51.1151	54.7719	50.5505	53.7507	50.5403	50.6953	50.8396	50.9354	51	40.8646	40.8646
47	343.759	52.7062	51.1935	54.4951	50.5961	52.6699	50.5546	50.6949	50.8358	50.9329	51	38.6221	38.6221
48	355.439	52.7077	51.3295	53.8277	50.6866	50.4626	50.5868	50.6968	50.8294	50.9282	51	34.5336	34.5336
49	361.279	52.6756	51.4173	53.4439	50.7307	49.3584	50.6045	50.6991	50.8255	50.9248	51	32.7289	32.7289
50	365	52.644	51.4173	53.1843	50.7581	48.6618	50.6162	50.701	50.8255	50.9248	51	30.9016	30.9016

Mail

Copy Tables



1:26 AM



Polymath Report

Complete action using



Send via Bluetooth



Gmail



Mail



Always

Just once

33	244.479	49.9593	4	51	74.2191	74.2191
34	250.319	50.1832	4	51	73.1718	73.1718
35	256.159	50.4093	4	51	71.9007	71.9007
36	267.839	50.8595	4	51	68.7402	68.7402
37	273.679	51.0791	5	51	66.8827	66.8827
38	279.519	51.2923	5	51	64.8649	64.8649
39	285.359	51.497	5	51	62.7071	62.7071
40	297.039	51.8731	5	51	58.0597	58.0597
41	302.879	52.0408	5	51	55.6171	55.6171
42	308.719	52.1928	5	51	53.1279	53.1279
43	314.559	52.3277	5	51	50.6173	50.6173
44	326.239	52.541	5	51	45.6328	45.6328
45	332.079	52.6174	5	51	43.2093	43.2093
46	337.919	52.6726	5	51	40.8646	40.8646
47	343.759	52.7062	5	51	38.6221	38.6221
48	355.439	52.7077	5	51	34.5336	34.5336
49	361.279	52.6756	51.3858	53.4439	50.7307	49.3584
50	365	52.644	51.4173	53.1843	50.7581	48.6618



1:28 AM

All



Search



Play Store



Menu



Music



My Verizon
Mobile



Navigation



NFL Mobile



Norton
Utilities



Notes



OliveOffice
Premium



People



Phone



Play Books



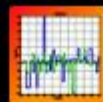
Play Movies
& TV



Play Music



Play Store



Plotim



Polymath



Qr Barcode
Scanner



Reign of
Amira



Settings



Setup
Wizard



Slacker



3/4



All



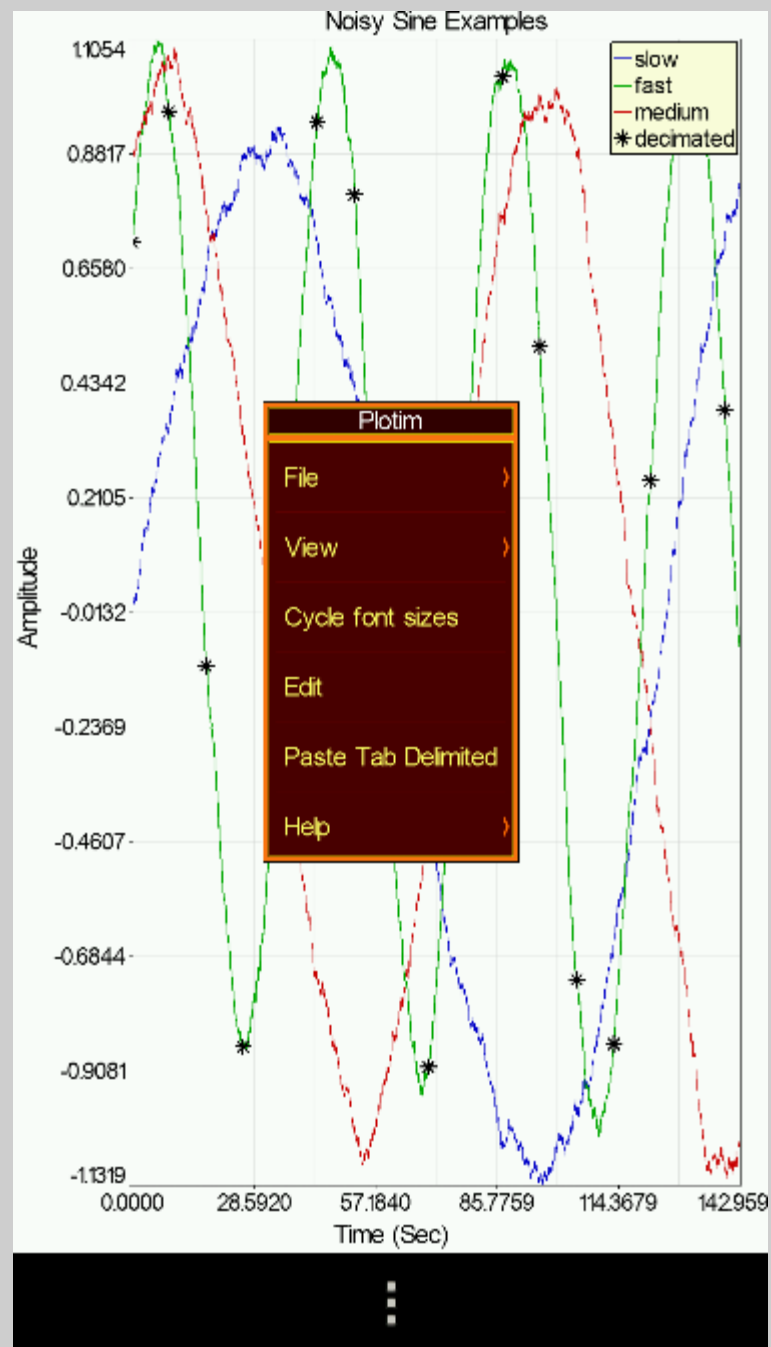
Frequent

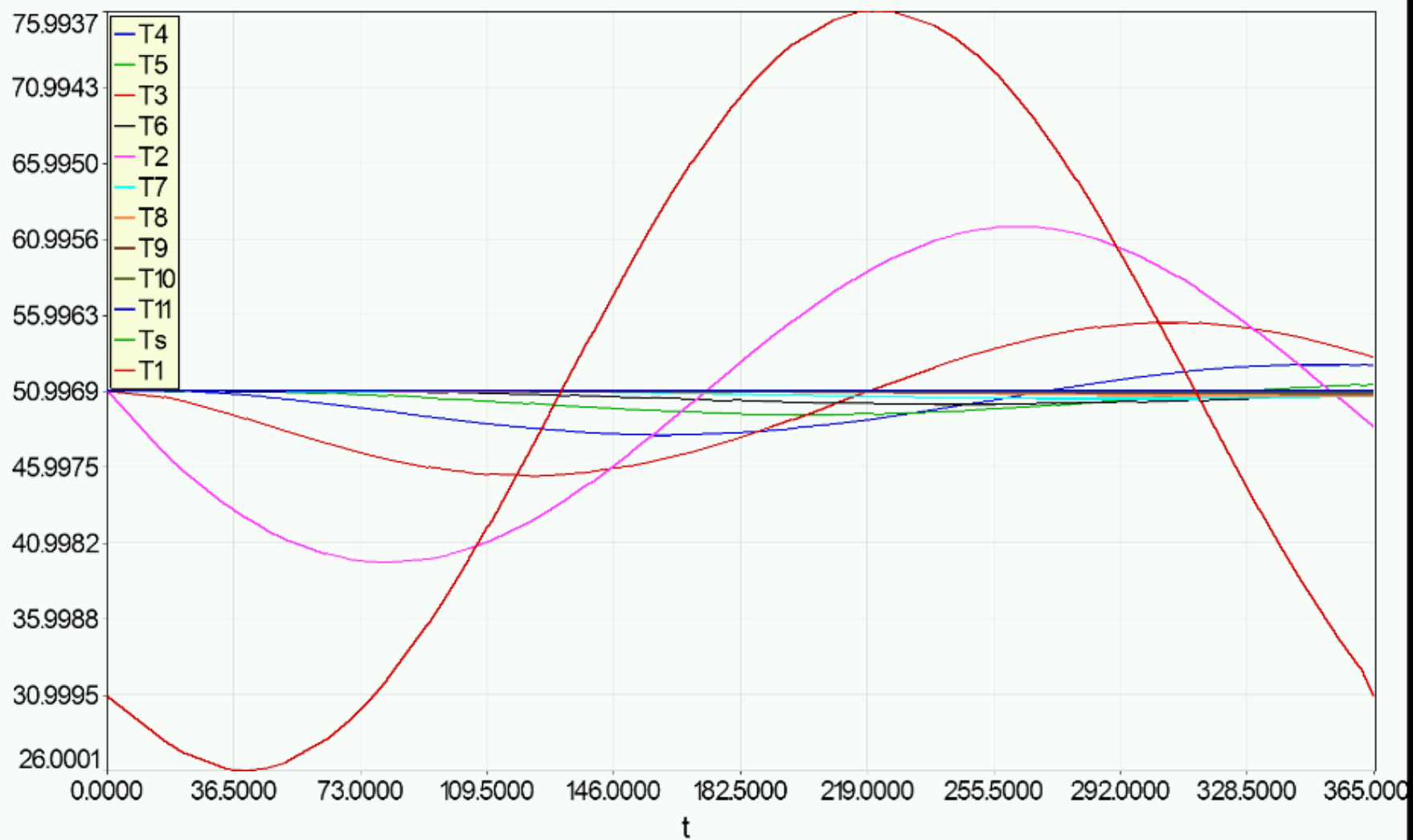


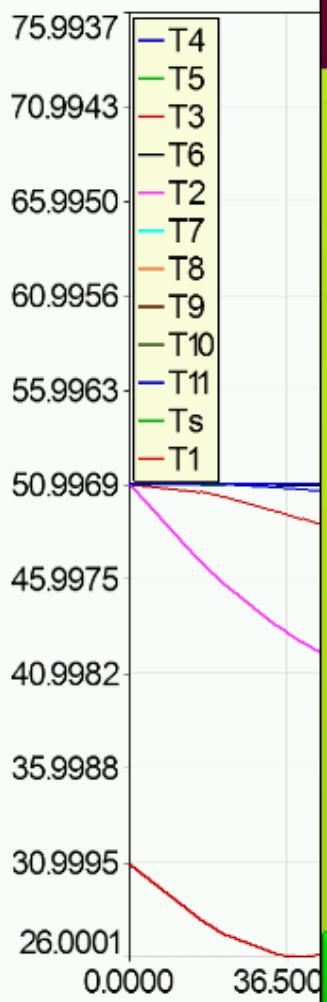
Downloads



Verizon apps

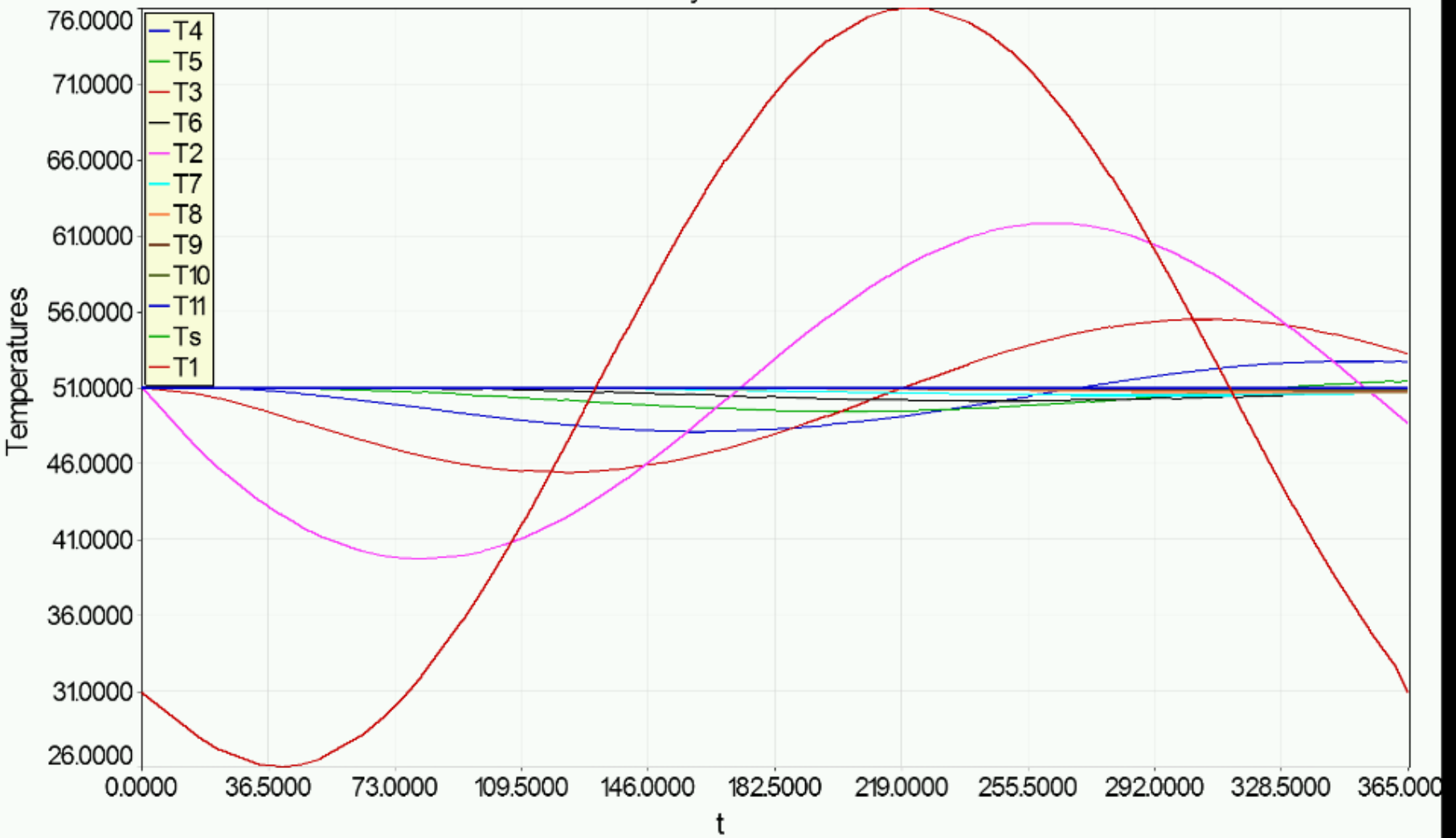






Plot descriptions		
Title		
X Label	t	
Y Label		
Plot1	,-,0,1,wid=3,name=T4	☒
Plot2	,-,0,2,wid=3,name=T5	☒
Plot3	,-,0,3,wid=3,name=T3	☒
Plot4	,-,0,4,wid=3,name=T6	☒
Plot5	,-,0,5,wid=3,name=T2	☒
Plot6	,-,0,6,wid=3,name=T7	☒
Update Autofill Cancel ?		







Polymath Sample Programs



Ex. 4 - Single NLE

Terminal Velocity



Ex. 5 - NLE System

Reaction Equilibrium



Ex. 6 (a) - Fitting Polynomials

Pressure Data



Ex. 6 (b) - Linear Regression

Pressure Data



Ex. 6 (c) - Nonlinear Regression

Pressure Data



Ex. 7 - ODE System

Heat Exchange



Run

Sample

Open

1



Ex. 6 (c) - Nonlinear Regression

Pressure Data

Verified Solution: $A = 5.76735$, $B = 677.094$, $C = 153.885$

Ref.: Comput. Appl. Eng. Educ. 6: 173, 1998

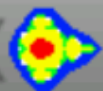
$TC = [-36.7, -19.6, -11.5, -2.6, 7.6, 15.4, 26.1, 42.2, 60.6, 80.1]$

$P = [1, 5, 10, 20, 40, 60, 100, 200, 400, 760]$

$\log P = \log(P)$

$\text{nlinfit } \log P = A - B / (C + TC)$

$m(\Delta) = 8.752$



Polymath Report

REG

2013-Jun-15

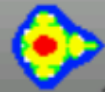
Model: $\log P = A - B / (C + TC)$

□
□
□

R^2	R^2adj	Rmsd	Variance
0.9996879	0.9995987	0.0047228	0.0003186

Source data points and calculated data points

	To	by	at	at	at	at	at
--	----	----	----	----	----	----	----



Run

Sample

Open

6

π verified solution. $A = 8.752$, $B = 2035$, $C = 273$

Ref.: Comput. Appl. Eng. Educ. 6: 173, 1998

$TC = [-36.7, -19.6, -11.5, -2.6, 7.6, 15.4, 26.1, 42.2, 60.6, 80.1]$

$P = [1, 5, 10, 20, 40, 60, 100, 200, 400, 560]$

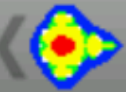
$\log P = \log(P)$

$\text{nlinfit } \log P = A - B / (C + TC)$

$m(A) = 8.752$

$m(B) = 2035$

$m(C) = 273$



Polymath Sample Programs



Ex. 1 - Linear Eqs.

Steady State Material Balances



Ex. 2 - Single NLE

Molar Volume and Compress... Van Der Waals



Ex. 3 - NLE System

Three Phase Equilib.



Ex. 4 - Single NLE

Terminal Velocity



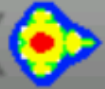
Ex. 5 - NLE System

Reaction Equilibrium



Ex. 6 (a) - Fitting Polynomials

Pressure Data



Polymath Sample Programs



Ex. 6 (b) - Linear Regression

Pressure Data



Ex. 6 (c) - Nonlinear Regression

Pressure Data



Ex. 7 - ODE System

Heat Exchange



Ex. 8- Boundary Value ODE System

Diffusion with Reaction



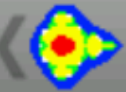
Ex. 9 - ODE System

Reversible Reaction in a PBR



Ex. 10(a) - ODE System

Dynamics of Heated Tank-Open loop



Polymath Sample Programs



Ex. 10(b) - ODE System

Dynamics of Heated Tank-Closed loop



Ex. 10(c) - ODE System

Dynamics of Heated Tank-limits on energy input



Ex. 11(a) - Single NLE

Initial Bubble Point.



Ex. 11(b) - DAE System

Binary Batch Distillation



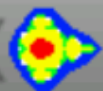
Ex. 12 - Single Partial Diff. Eq.

Unsteady State Heat Conduction.



Ex. 13 - Nonlinear Regression

Catalytic Reforming Reac.



Polymath Sample Programs



Ex. 11(b) - DAE System

Binary Batch Distillation



Ex. 12 - Single Partial Diff. Eq.

Unsteady State Heat Conduction.



Ex. 13 - Nonlinear Regression

Catalytic Reforming Reac.



Ex. 14(a) - Multi-Linear Regression

Heat of Hardening



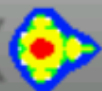
Ex. 14(b) - Multi-Linear Regression via origin

Heat of Hardening



Ex. 15 - Linear Eqs.

Biological Reactors



Polymath Sample Programs

Heat of Hardening



Ex. 15 - Linear Eqs.

Biological Reactors



Ex. 16 - Stiff ODE System

Biological Reactors



Ex. 17 - NLE System

Combustion of Propane



Ex. 18 - NLE System

Complex Chemical Equilibrium



Ex. 19 - Consecutive calculations

Gas pressure from SRK equation of state



Ex. 20 - Consecutive calculations

Physical property calculator for liquid CO₂